I asked the same question in their FAQ on their forum.

Feign death (basically faking your own death) is an addition to the game. Therefore you can use feign death to fool other players that you are dead. Obviously, if your body disappeared right after you die, then feigning death would be completely useless.

Therefore that means that your bodies will linger on the battlefield for a while after you die.